

**Example 13.4**  
**Design of continuous flight auger piles from cone tests**  
**Verification of strength (limit state GEO)**

Design situation

Consider the design of continuous flight auger (CFA) piles for a site in Twickenham, London. Ground conditions at the site comprise dense, becoming loose gravelly, SAND. Cone penetration tests have been performed at the site to a depth of 8m. (Data courtesy CL Associates.) The limiting average unit shaft resistance  $p_s$  and limiting unit base resistance  $p_b$  at each cone location are estimated to be:

$$p_s = \begin{pmatrix} 120\text{kPa} \\ 120\text{kPa} \\ 100\text{kPa} \\ 120\text{kPa} \end{pmatrix} \quad p_b = \begin{pmatrix} 2800\text{kPa} \\ 3000\text{kPa} \\ 2000\text{kPa} \\ 3000\text{kPa} \end{pmatrix} \quad \textcircled{1}$$

A group of  $N = 6$  piles with diameter  $D = 400\text{mm}$  and length  $L = 6\text{m}$  are required to carry between them a permanent action  $F_{Gk} = 2100\text{kN}$  together with a variable action  $F_{Qk} = 750\text{kN}$ . The weight density of reinforced concrete is  $\gamma_{ck} = 25 \frac{\text{kN}}{\text{m}^3}$  (as per EN 1991-1-1 Table A.1).

Design Approach 1

Actions and effects

The self-weight of pile is  $W_{Gk} = \left( \frac{\pi \times D^2}{4} \right) \times L \times \gamma_{ck} = 18.8 \text{ kN}$

Partial factors from Sets  $\begin{pmatrix} \text{A1} \\ \text{A2} \end{pmatrix}$ :  $\gamma_G = \begin{pmatrix} 1.35 \\ 1 \end{pmatrix}$  and  $\gamma_Q = \begin{pmatrix} 1.5 \\ 1.3 \end{pmatrix}$   $\textcircled{2}$

Design total action per pile is:

$$F_{cd} = \frac{\gamma_G \times (F_{Gk} + W_{Gk}) + \gamma_Q \times F_{Qk}}{N} = \begin{pmatrix} 664 \\ 516 \end{pmatrix} \text{ kN}$$

Calculated shaft resistance

Number of cone penetration tests  $n = 4$

Calculated shaft resistance  $R_s = \pi \times D \times L \times p_s = \begin{pmatrix} 905 \\ 905 \\ 754 \\ 905 \end{pmatrix}$  kN

$$\sum R_s$$

Mean calculated shaft resistance  $R_{s,mean} = \frac{\sum R_s}{n} = 867$  kN

Minimum calculated shaft resistance  $R_{s,min} = \min(R_s) = 754$  kN

#### Calculated base resistance

Calculated base resistance  $R_b = \left( \frac{\pi \times D^2}{4} \right) \times p_b = \begin{pmatrix} 352 \\ 377 \\ 251 \\ 377 \end{pmatrix}$  kN

$$\sum R_b$$

Mean calculated base resistance  $R_{b,mean} = \frac{\sum R_b}{n} = 339$  kN

Minimum calculated base resistance  $R_{b,min} = \min(R_b) = 251$  kN

#### Calculated total resistance

Mean calculated total resistance  $R_{t,mean} = R_{s,mean} + R_{b,mean} = 1206$  kN

Minimum calculated total resistance  $R_{t,min} = R_{s,min} + R_{b,min} = 1005$  kN

#### Characteristic resistance

Correlation factor on mean measured resistance  $\xi_3 = 1.31$  **3**

Correlation factor on minimum measured resistance  $\xi_4 = 1.20$  **3**

For a pile group that can transfer load from weak to strong piles (S7.6.2.2.(9)),  $\xi$  may be divided by 1.1 (but  $\xi_3$  cannot fall beneath 1.0).

Thus  $\xi_3 = \max\left(\frac{\xi_3}{1.1}, 1.0\right) = 1.19$  and  $\xi_4 = \frac{\xi_4}{1.1} = 1.09$

Calculated resistances  $\frac{R_{t,mean}}{\xi_3} = 1013$  kN and  $\frac{R_{t,min}}{\xi_4} = 922$  kN **4**

Characteristic resistance should therefore be based on the minimum value.

$$\text{Characteristic shaft resistance is } R_{sk} = \frac{R_{s,min}}{\xi_4} = 691 \text{ kN} \quad 5$$

$$\text{Characteristic base resistance is } R_{bk} = \frac{R_{b,min}}{\xi_4} = 230 \text{ kN} \quad 5$$

#### Design resistance

Partial factors from Sets  $\begin{pmatrix} R1 \\ R4 \end{pmatrix}$ :  $\gamma_s = \begin{pmatrix} 1 \\ 1.3 \end{pmatrix}$  and  $\gamma_b = \begin{pmatrix} 1.1 \\ 1.45 \end{pmatrix}$  5

$$\text{Design resistance is } R_{cd} = \frac{R_{sk}}{\gamma_s} + \frac{R_{bk}}{\gamma_b} = \begin{pmatrix} 901 \\ 691 \end{pmatrix} \text{ kN}$$

#### Verification of compression resistance

$$\text{Degree of utilization } \lambda_{GEO,1} = \frac{F_{cd}}{R_{cd}} = \begin{pmatrix} 74 \\ 75 \end{pmatrix} \% \quad 6$$

Design is unacceptable if degree of utilization is > 100%

#### Design Approach 2

##### Actions and effects

Partial factors from set A1:  $\gamma_G = 1.35$  and  $\gamma_Q = 1.5$  2

$$\text{Design total action per pile is } F_{cd} = \frac{\gamma_G \times (F_{Gk} + W_{Gk}) + \gamma_Q \times F_{Qk}}{N} = 664 \text{ kN}$$

#### Design resistance

Characteristic shaft and base resistances are unchanged from DA1

Partial factors from set R2:  $\gamma_s = 1.1$  and  $\gamma_b = 1.1$  7

$$\text{Design resistance is } R_{cd} = \frac{R_{sk}}{\gamma_s} + \frac{R_{bk}}{\gamma_b} = 838 \text{ kN}$$

### Verification of compression resistance

$$\text{Degree of utilization } \Delta_{GEO,2} = \frac{F_{cd}}{R_{cd}} = 79 \% \quad \textcircled{6}$$

Design is unacceptable if degree of utilization is > 100%

### Design Approach 3

#### Actions and effects

Partial factors from set A1:  $\gamma_G = 1.35$  and  $\gamma_Q = 1.5$  **2**

$$\text{Design total action per pile is } F_{cd} = \frac{\gamma_G \times (F_{Gk} + W_{Gk}) + \gamma_Q \times F_{Qk}}{N} = 664 \text{ kN}$$

#### Characteristic resistance

Partial factors from set M2 should be applied to material properties... but since there are no material properties to factor, we will factor the resistances instead using  $\gamma_\varphi = 1.25$ . Since resistances are governed by the minimum calculated resistance (as per DAs 1 and 2)...

$$\text{Characteristic shaft resistance is } R_{sk} = \frac{R_{s,min}}{\xi_4 \times \gamma_\varphi} = 553 \text{ kN}$$

$$\text{Characteristic base resistance is } R_{bk} = \frac{R_{b,min}}{\xi_4 \times \gamma_\varphi} = 184 \text{ kN}$$

#### Design resistance

Partial factors from set R3:  $\gamma_s = 1$  and  $\gamma_b = 1$

$$\text{Design resistance is } R_{cd} = \frac{R_{sk}}{\gamma_s} + \frac{R_{bk}}{\gamma_b} = 737 \text{ kN}$$

### Verification of compression resistance

$$\text{Degree of utilization } \Delta_{GEO,3} = \frac{F_{cd}}{R_{cd}} = 90 \% \quad \textcircled{6}$$

Design is unacceptable if degree of utilization is > 100%

## Design to UK National Annex to BS EN 1997-1

### Characteristic resistance

Correlation factor on mean measured resistance  $\xi_3 = 1.38$  ⑧

Correlation factor on minimum measured resistance  $\xi_4 = 1.29$  ⑧

For a pile group that can transfer load from weak to strong piles (§7.6.2.2.(9)),  $\xi$  may be divided by 1.1 (but  $\xi_3$  cannot fall beneath 1.0).

$$\text{Thus } \xi_3 = \max\left(\frac{\xi_3}{1.1}, 1.0\right) = 1.25 \text{ and } \xi_4 = \frac{\xi_4}{1.1} = 1.17$$

$$\text{Calculated resistances } \frac{R_{t,\text{mean}}}{\xi_3} = 961.6 \text{ kN and } \frac{R_{t,\text{min}}}{\xi_4} = 857 \text{ kN} \quad \text{④}$$

Characteristic resistance should therefore be based on the minimum value, so...

$$\text{Characteristic shaft resistance is } R_{sk} = \frac{R_{s,\text{min}}}{\xi_4} = 643 \text{ kN}$$

$$\text{Characteristic base resistance is } R_{bk} = \frac{R_{b,\text{min}}}{\xi_4} = 214 \text{ kN}$$

### Design resistance

$$\text{Partial factors from Sets } \begin{pmatrix} R1 \\ R4 \end{pmatrix}: \gamma_s = \begin{pmatrix} 1 \\ 1.6 \end{pmatrix} \text{ and } \gamma_b = \begin{pmatrix} 1 \\ 2 \end{pmatrix} \quad \text{⑨}$$

$$\text{Design resistance is } R_{cd} = \frac{R_{sk}}{\gamma_s} + \frac{R_{bk}}{\gamma_b} = \begin{pmatrix} 857 \\ 509 \end{pmatrix} \text{ kN}$$

### Verification of compression resistance

$$\text{Degree of utilization } \Delta_{GEO,1} = \frac{F_{cd}}{R_{cd}} = \begin{pmatrix} 77 \\ 101 \end{pmatrix} \% \quad \text{⑩}$$

Design is unacceptable if degree of utilization is > 100%